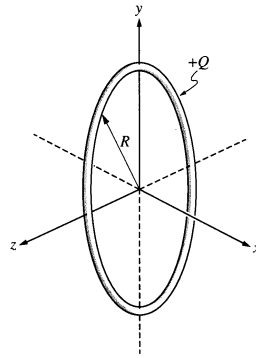


## Electrostatics 6



1999E3. The nonconducting ring of radius  $R$  shown above lies in the  $yz$ -plane and carries a uniformly distributed positive charge  $Q$ .

a. Determine the electric potential at points along the  $x$ -axis as a function of  $x$ .

b. i. Show that the  $x$ -component of the electric field along the  $x$ -axis is given by

$$E_x = \frac{Qx}{4\pi\epsilon_0(R^2 + x^2)^{\frac{3}{2}}}$$

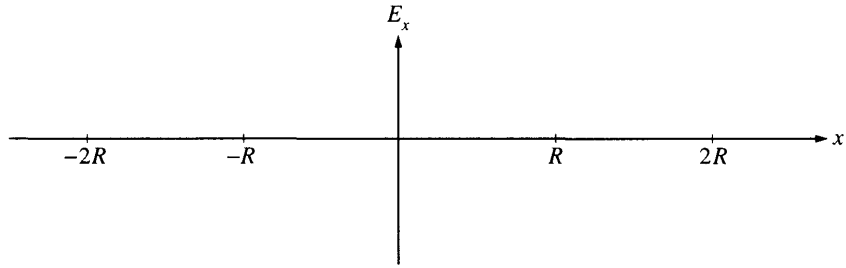
ii. What are the  $y$ - and  $z$ - components of the electric field along the  $x$ -axis?

c. Determine the following.

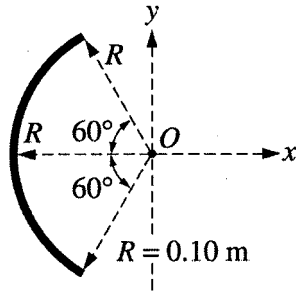
i. The value of  $x$  for which  $E_x$  is a maximum

ii. The maximum electric field  $E_{x \text{ max}}$

d. On the axes below, sketch  $E_x$  versus  $x$  for points on the  $x$ -axis from  $x = -2R$  to  $x = +2R$ .



- e. An electron is placed at  $x = R/2$  and released from rest. Qualitatively describe its subsequent motion.



2002E1. A rod of uniform linear charge density  $\lambda = +1.5 \times 10^{-5} \text{ C/m}$  is bent into an arc of radius  $R = 0.10 \text{ m}$ . The arc is placed with its center at the origin of the axes shown above.

- a. Determine the total charge on the rod.
  
- b. Determine the magnitude and direction of the electric field at the center O of the arc.
  
- c. Determine the electric potential at point O.

A proton is now placed at point O and held in place. Ignore the effects of gravity in the rest of this problem.

- d. Determine the magnitude and direction of the force that must be applied in order to keep the proton at rest.
  
- e. The proton is now released. Describe in words its motion for a long time after its release.