

## Momentum 5

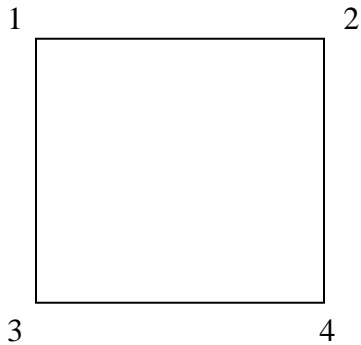
1. Find the location of the center of mass for the following three and four particle systems in one dimension (imagine the masses along a number line).

a. mass 1: 4 kg at  $x = 0$  m  
mass 2: 4 kg at  $x = 5$  m  
mass 3: 4 kg at  $x = 10$  m

b. mass 1: 8 kg at  $x = 0$  m  
mass 2: 6 kg at  $x = 5$  m  
mass 3: 4 kg at  $x = 10$  m

c. mass 1: 4 kg at  $x = 0$  m  
mass 2: 4 kg at  $x = 2$  m  
mass 3: 4 kg at  $x = 10$  m

2. a. Find the center of mass of a system consisting of 4 masses each at the corners of a square with each side measuring 1 m. mass 1 = 3 kg, mass 2 = 3 kg, mass 3 = 3 kg, and mass 4 = 3 kg.



b. How would the center of mass move if masses 3 and 4 were doubled? Find the center of mass for that situation.

c. How would the center of mass move if mass 3 were removed (assume all masses are now 3 kg)? Find the center of mass for that situation.

3. Find the velocity of the center of mass for mass 1 = 5 kg moving at 15 m/s and mass 2 = 2 kg moving at -20 m/s? What would happen to the velocity of the center of mass if these two objects were to collide?

4. a. What is the velocity of the center of mass of a system containing the following masses: a 3 kg mass traveling at 8 m/s and a 4 kg mass traveling in the opposite direction with a speed of 6 m/s?
- b. What would happen if the two objects hit and stuck together? What would the final velocity of the system of masses be?
- c. What is the momentum of each mass before they hit?
- d. What is the total momentum of the system?
5. Two ice-skaters ( $m_1=60$  kg,  $m_2=80$  kg) are standing next to each other and moving with a velocity of 3 m/s. They push off of each other.
- a. What is the velocity of the center of mass before they push off of each other?
- b. What happens to the velocity of the center of mass when they push off of each other? Why?
- c. Skater 1 moves away with a velocity of 3 m/s in the opposite direction than they were traveling. What is the velocity of skater 2?
- d. What is the velocity of skater 1 with respect to the center of mass?
- d. What is the velocity of skater 2 with respect to the center of mass?
6. Two bowling balls of equal mass collide. Ball 1 is initially moving with a velocity of 10 m/s and ball 2 is initially at rest.
- a. Find the velocity of ball 2 if ball 1 moves with a velocity of -3 m/s after the collision.
- b. Find the velocity of ball 2 if ball 1 moves with a velocity of 5 m/s after the collision.
- c. Find the velocity of ball 2 if ball 1 is at rest after the collision.